# Time-Frequency analysis of biophysical time series

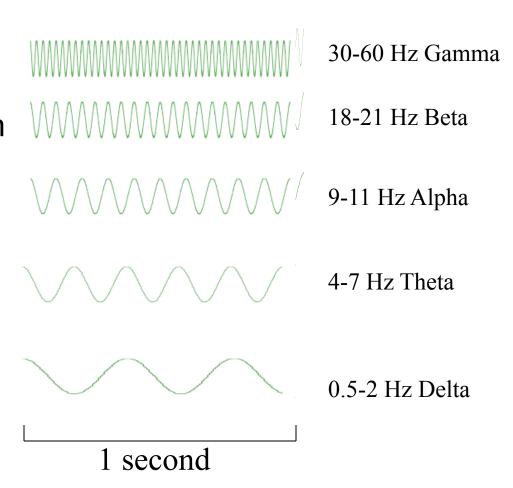
Nov 18th 2010, 12th EEGLAB workshop

**Arnaud Delorme** 

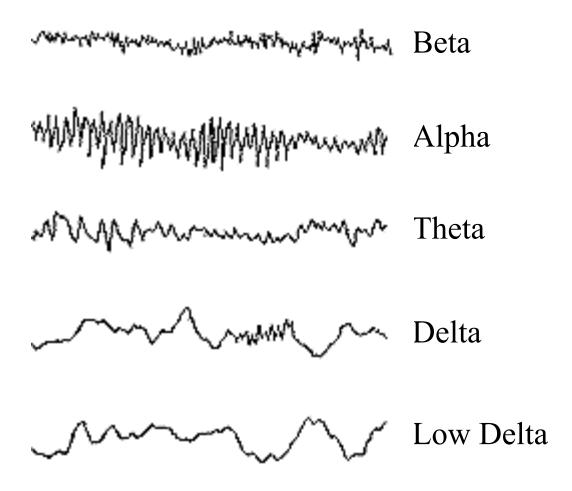
SCCN, UCSD CERCO, CNRS

## Frequency analysis

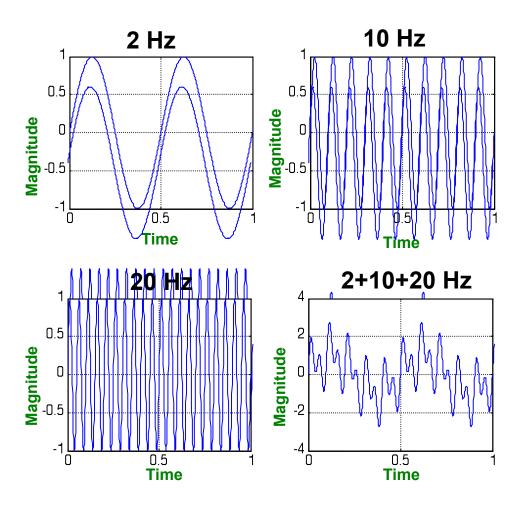
synchronicity of cell excitation determines amplitude and rhythm of the EEG signal



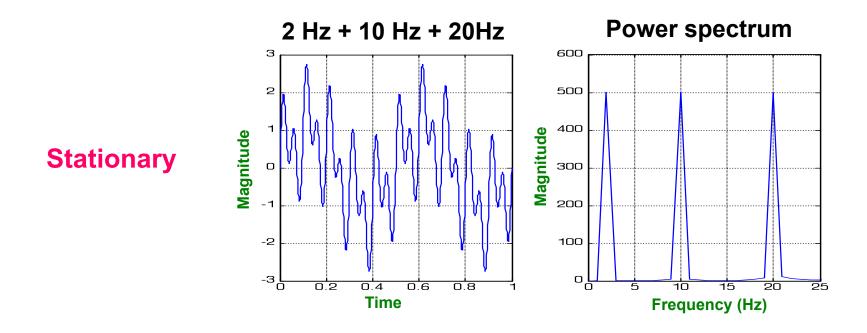
## Frequency analysis



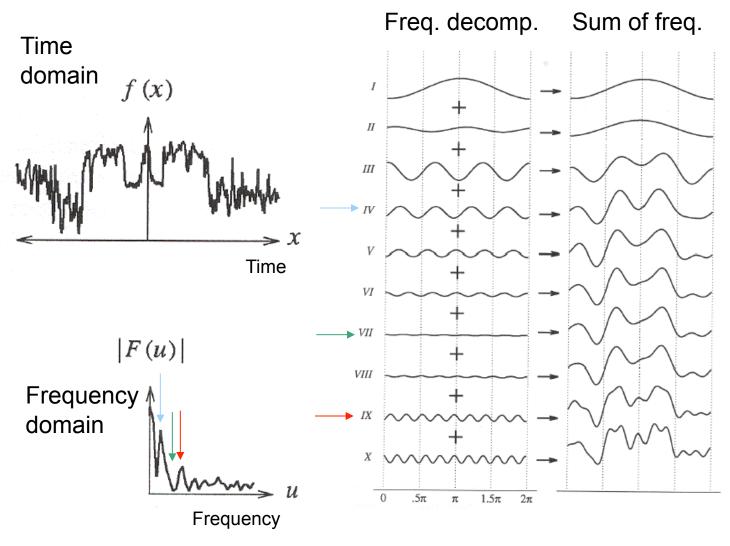
## Stationary signals



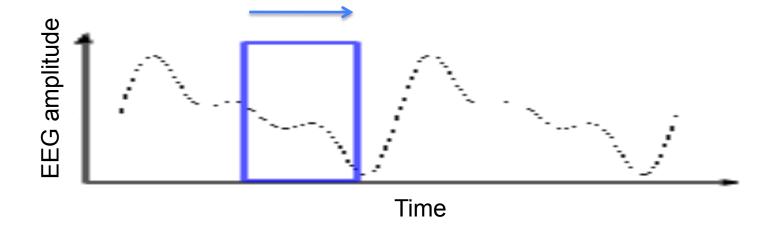
## Stationary signal

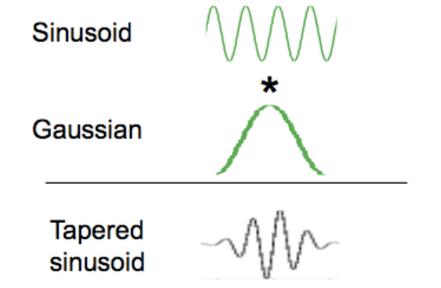


By looking at the Power spectrum of the signal we can recognize three frequency Components (at 2,10,20Hz respectively).



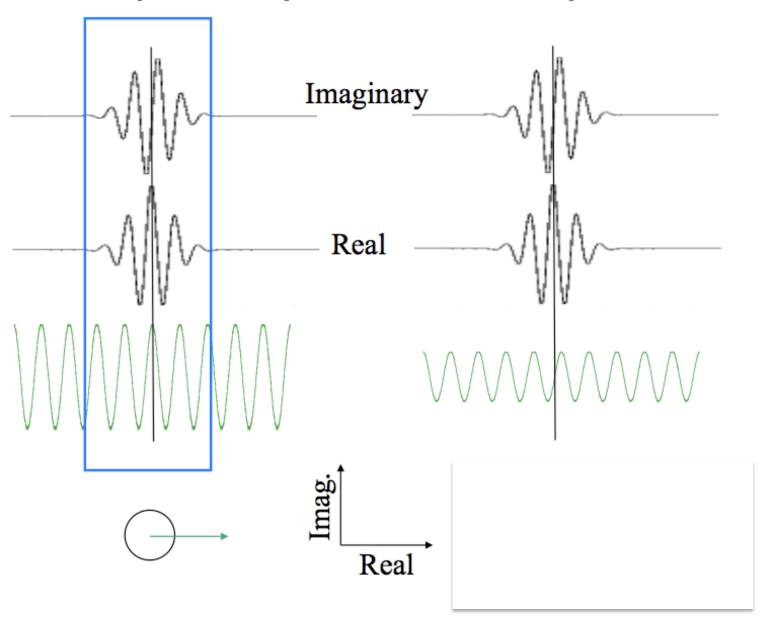
Forward transform  $F(u) = \int_{-\infty}^{+\infty} f(x)e^{-2\pi i u x} dx$ Inverse transform  $f(x) = \int_{-\infty}^{+\infty} F(u)e^{2\pi i u x} du$ 



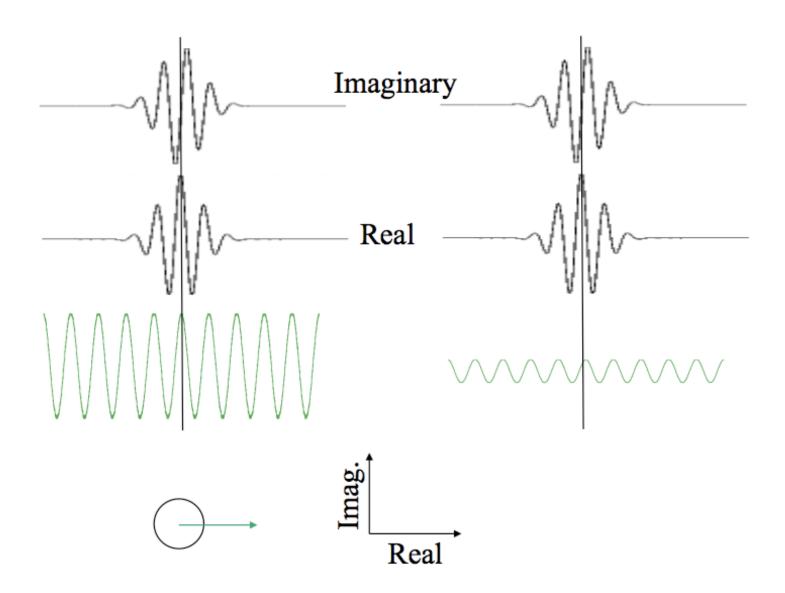


Performing Fourier transform by using a time moving window

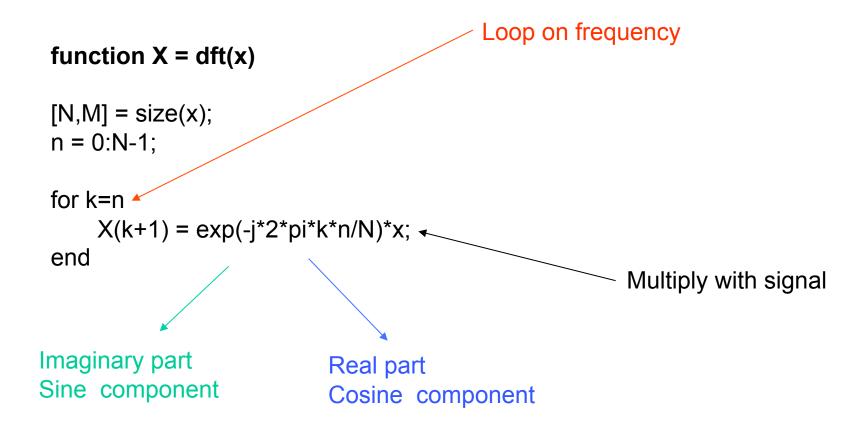
## Spectral phase and amplitude

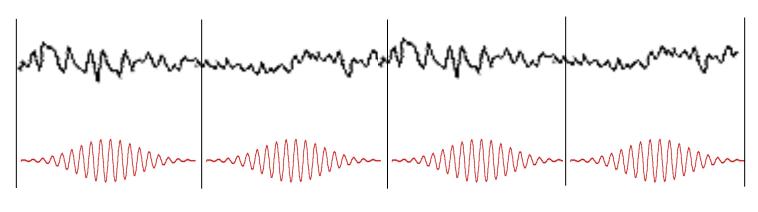


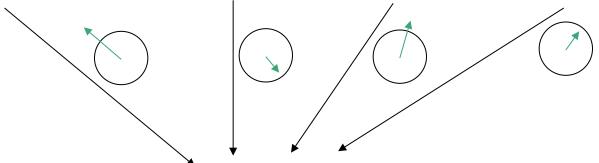
## Spectral phase and amplitude



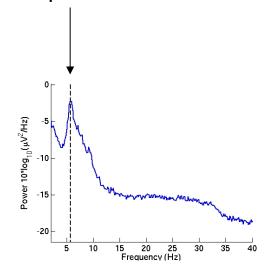
#### **Discrete Fourrier Transform function**



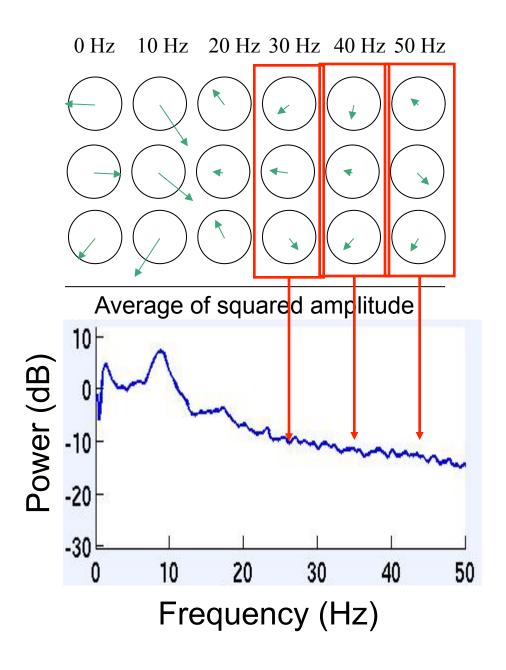


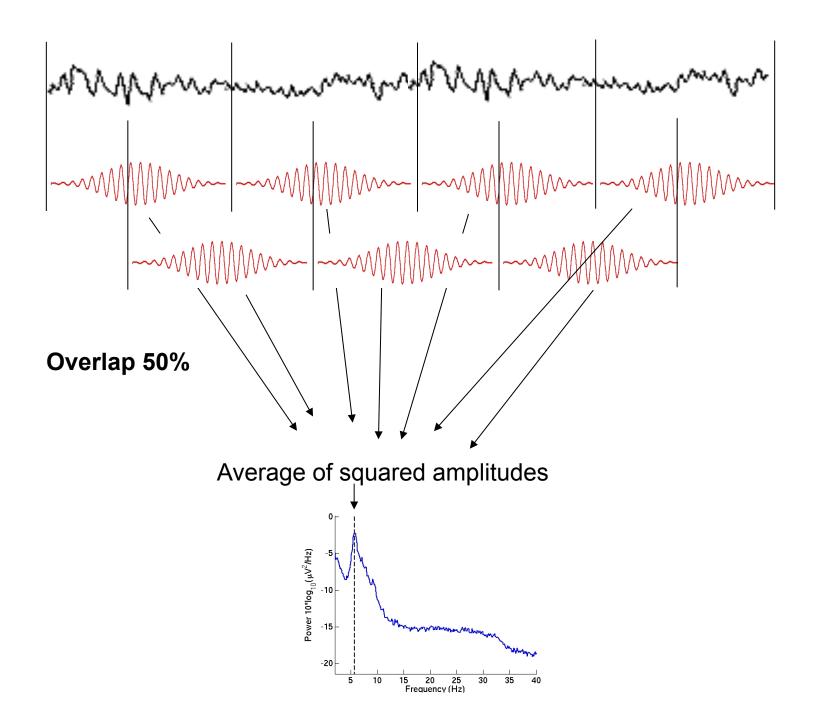


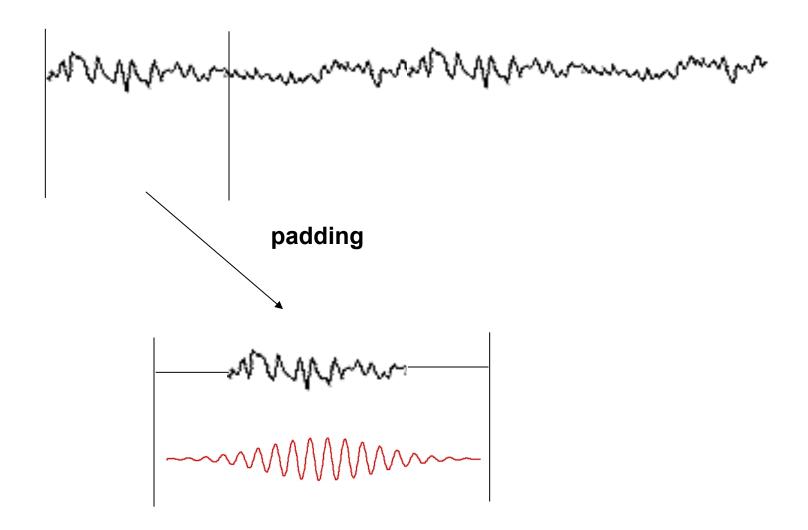
Average of squared absolute values



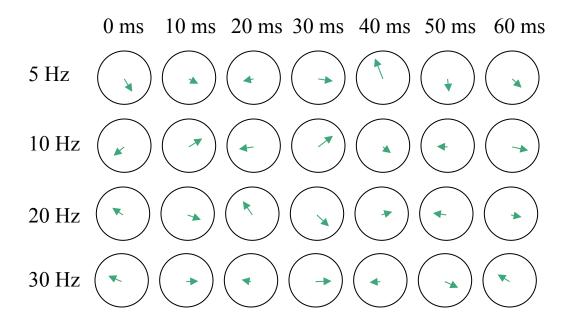
## Spectral power



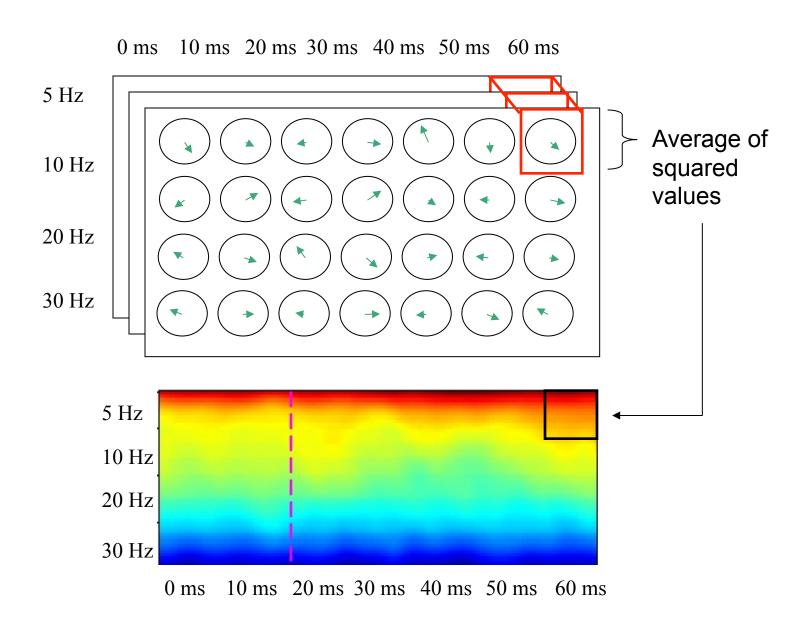




## Spectrogram or ERSP



## Spectrogram or ERSP

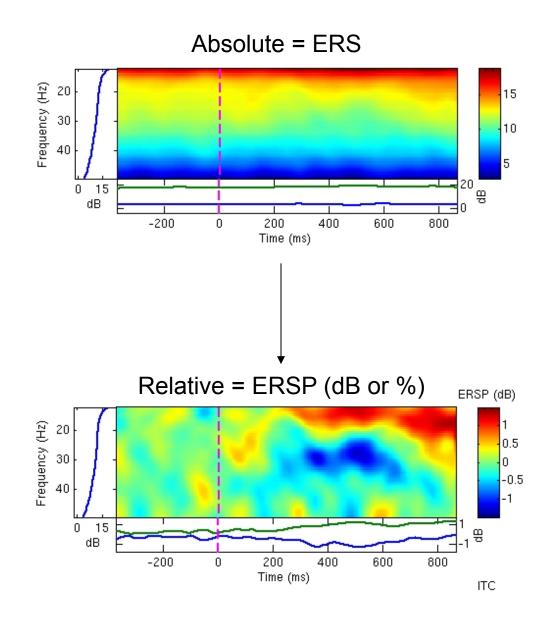


# Power spectrum and event-related spectral perturbation

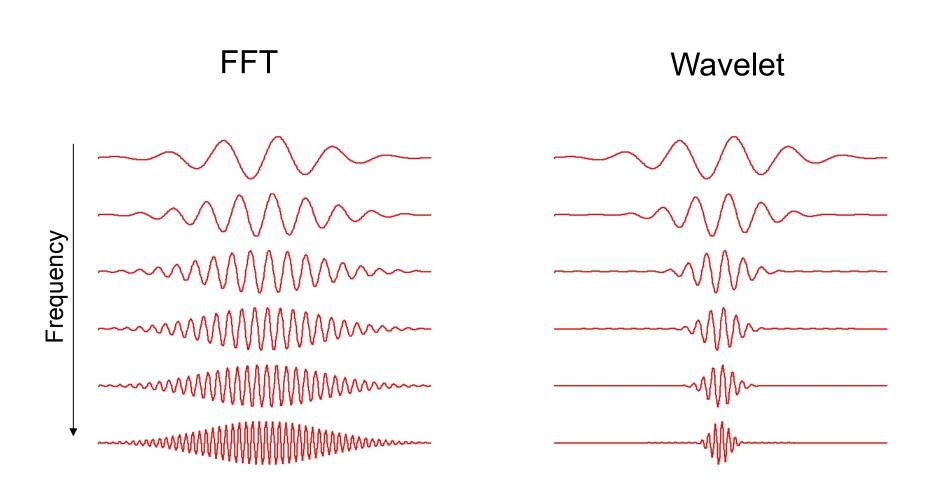
ERS 
$$(f,t) = \frac{1}{n} \sum_{k=1}^{n} |F_k(f,t)|^2$$
Complex number

Scaled to dB 10Log<sub>10</sub>(ERSP)

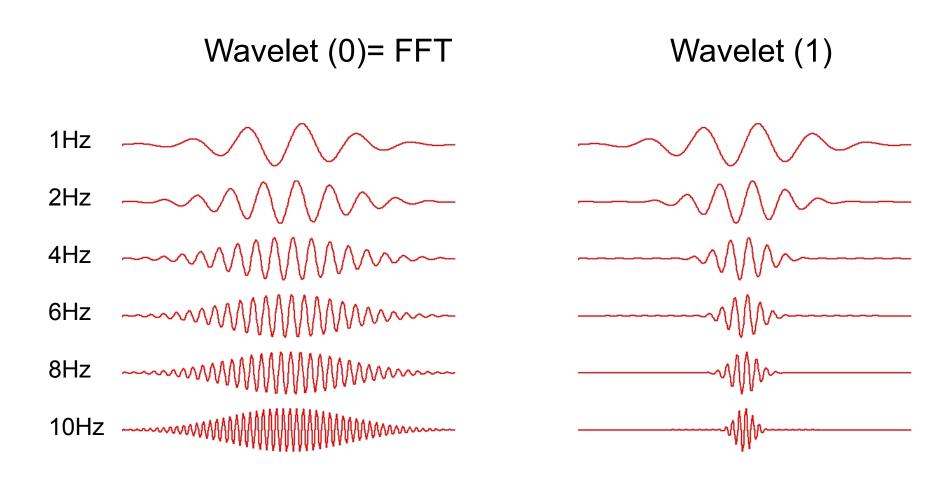
## Absolute versus relative power



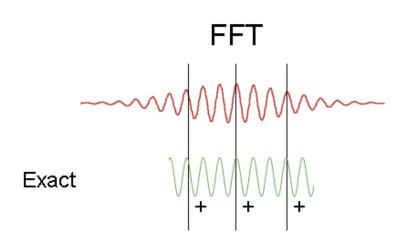
#### Difference between FFT and wavelets

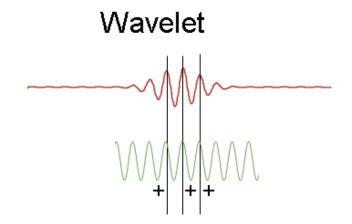


#### Wavelets factor



## Time-frequency resolution trade off

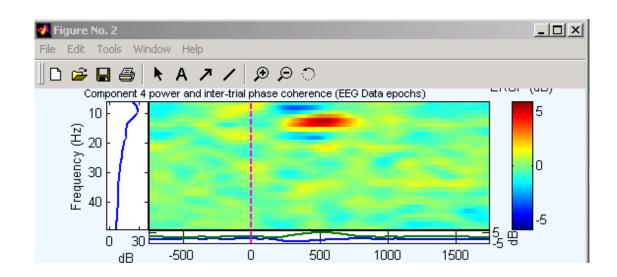




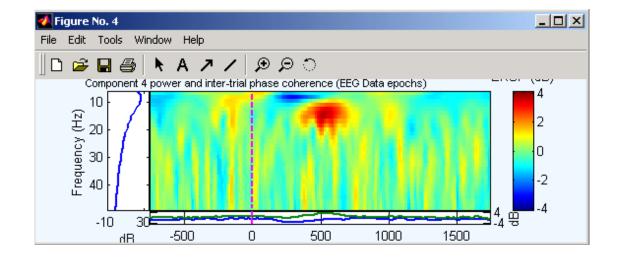
High freq. resolution low time-resolution

Low freq. resolution high time-resolution

### FFT



#### Pure wavelet



## The Uncertainty Principle

A signal <u>cannot</u> be localized arbitrarily well <u>both</u> in time/ position <u>and</u> in frequency/ momentum.

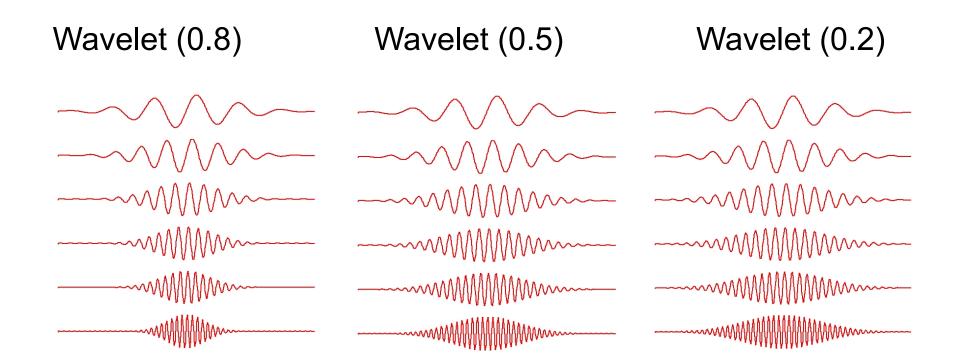
There exists a lower bound to the *Heisenberg's product:* 

$$\Delta t \Delta f \ge 1/(4\pi)$$



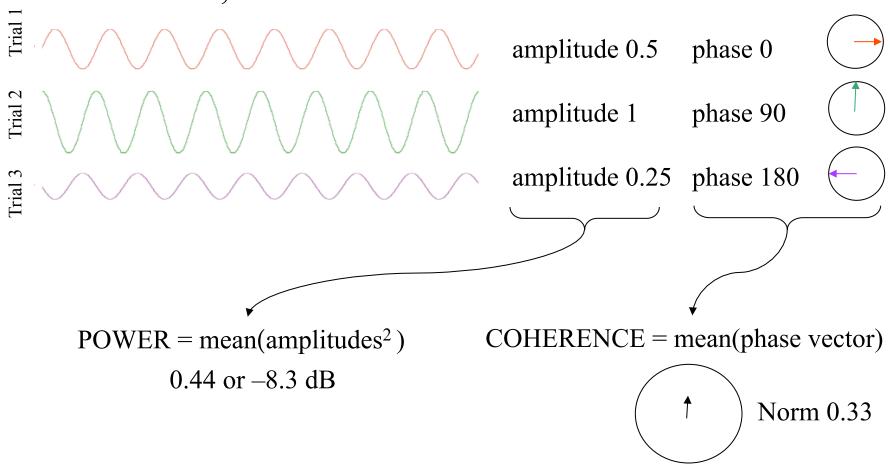
 $\Delta f = 1$ Hz,  $\Delta t = 80$  msec or  $\Delta f = 2$ Hz,  $\Delta t = 40$  msec

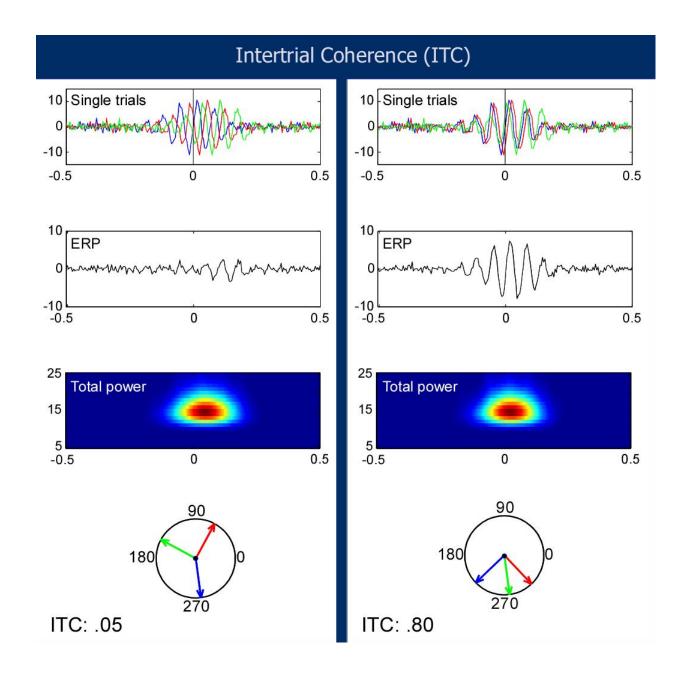
#### Modified wavelets



#### Inter trial coherence

#### same time, different trials



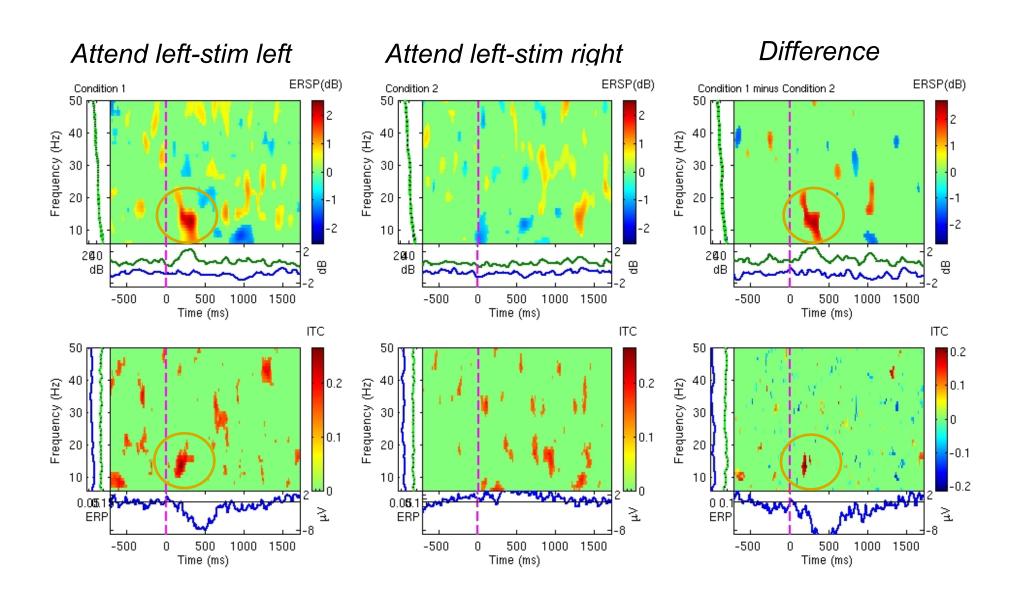


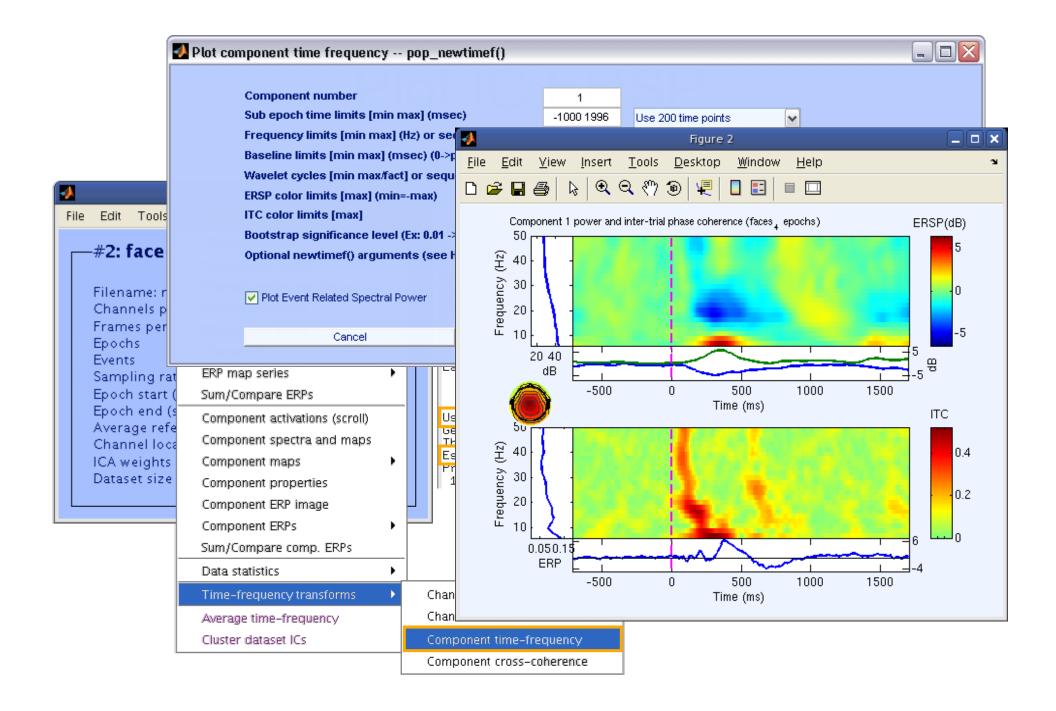
#### Phase ITC

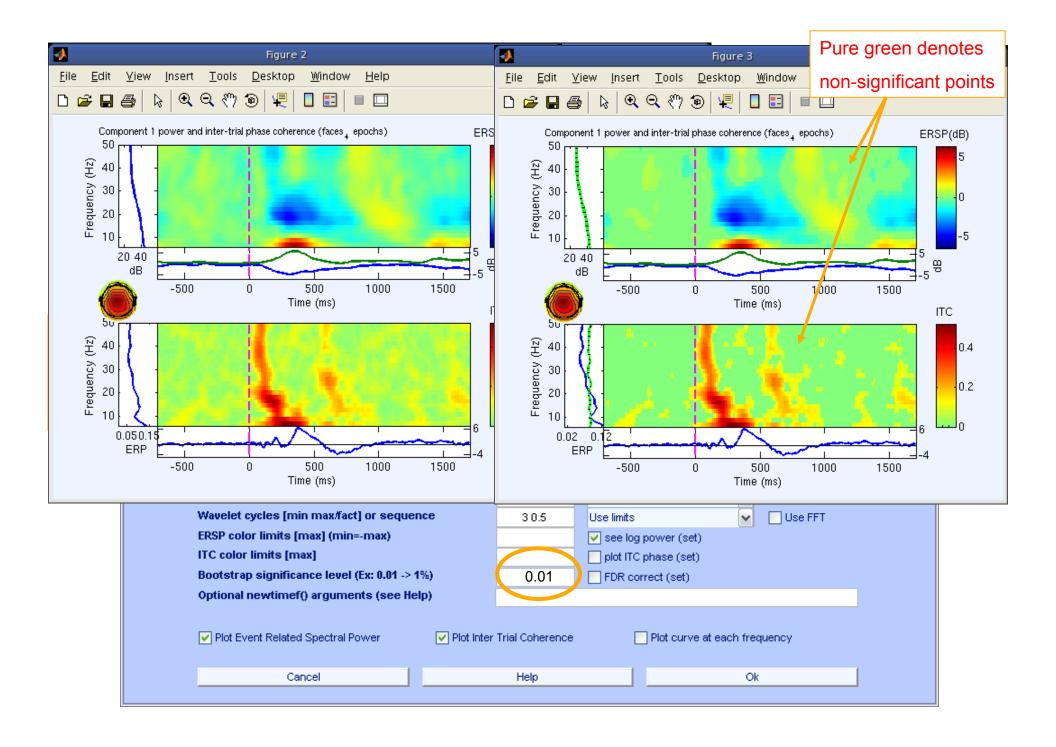
$$ITPC(f,t) = \frac{1}{n} \sum_{k=1}^{n} \frac{F_k(f,t)}{|F_k(f,t)|}$$

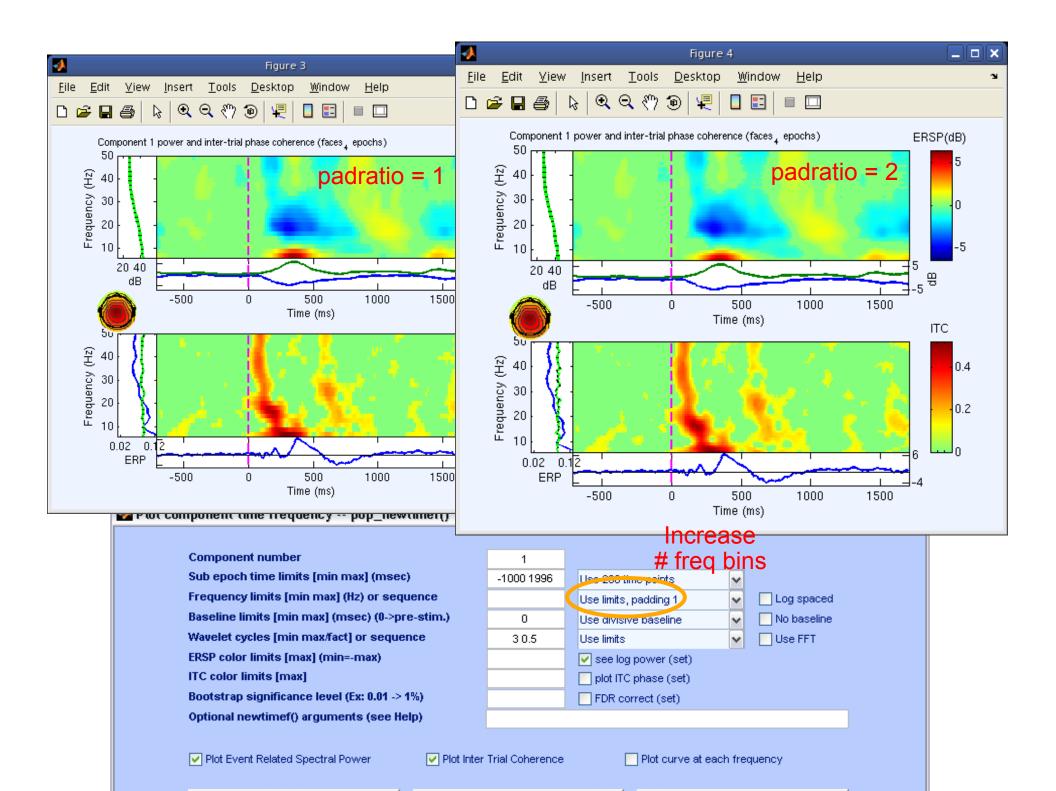
Normalized (no amplitude information)

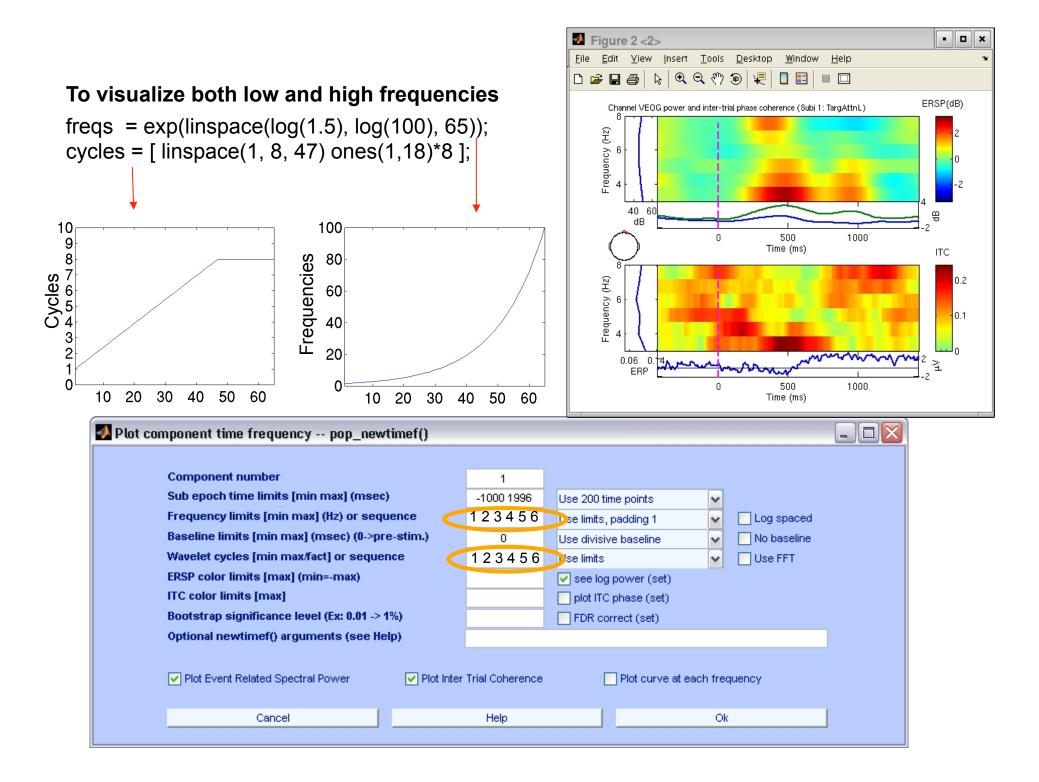
#### Power and inter trial coherence



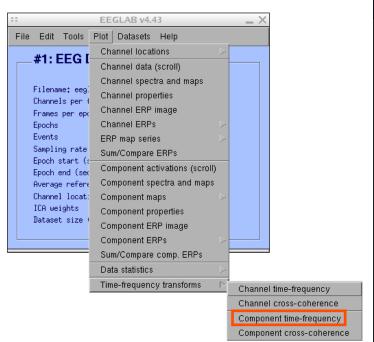


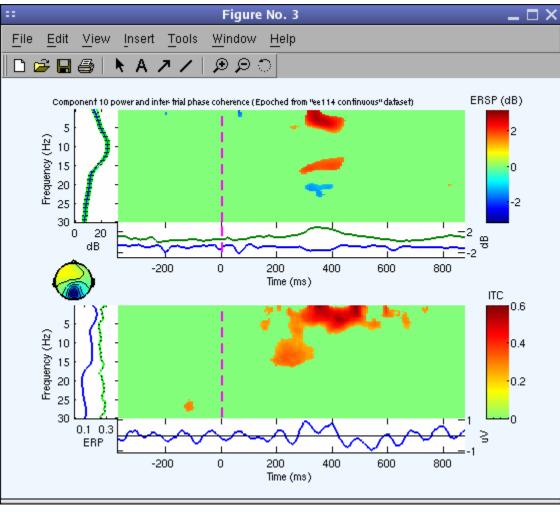






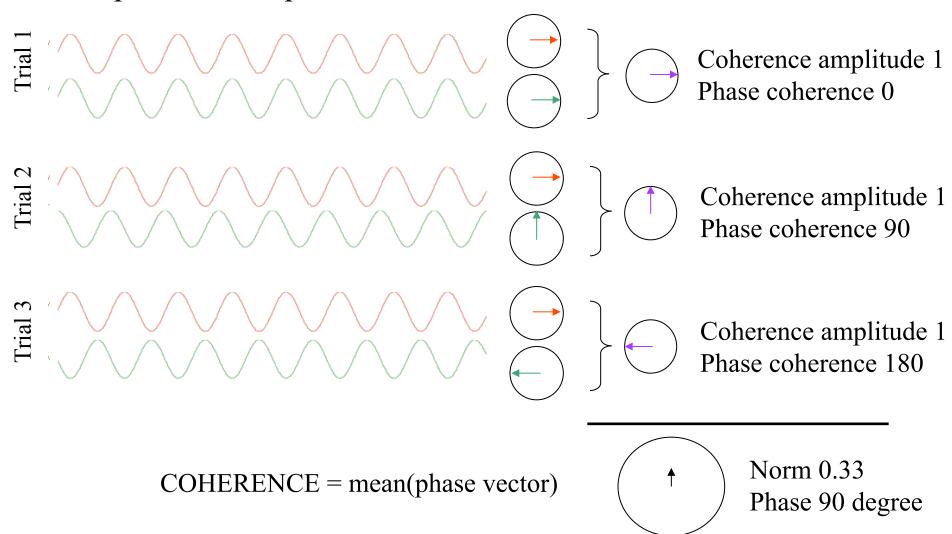
## Component time-frequency



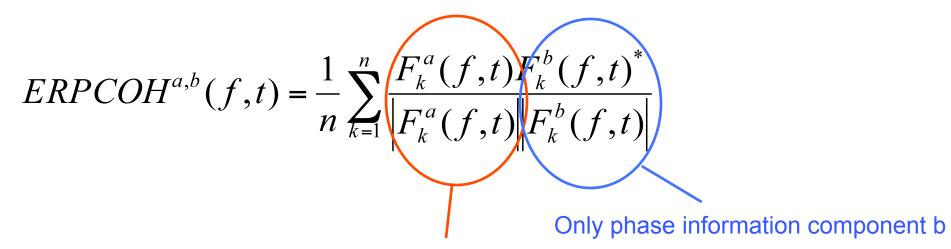


## Cross-coherence amplitude and phase

2 components, comparison on the same trials

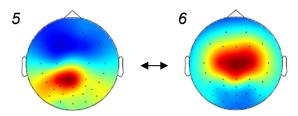


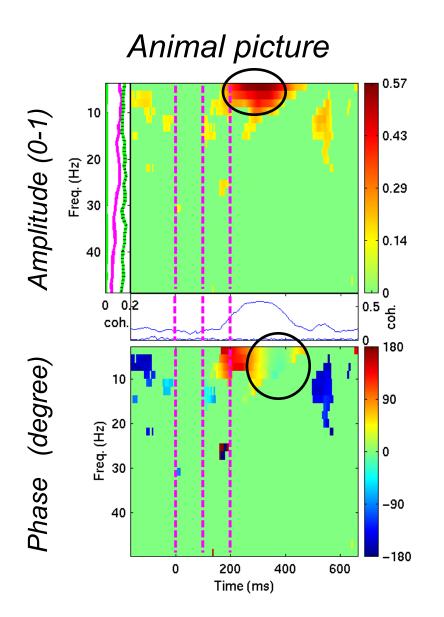
## Phase coherence (default)

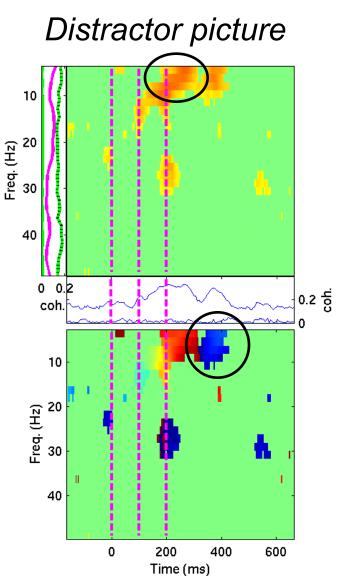


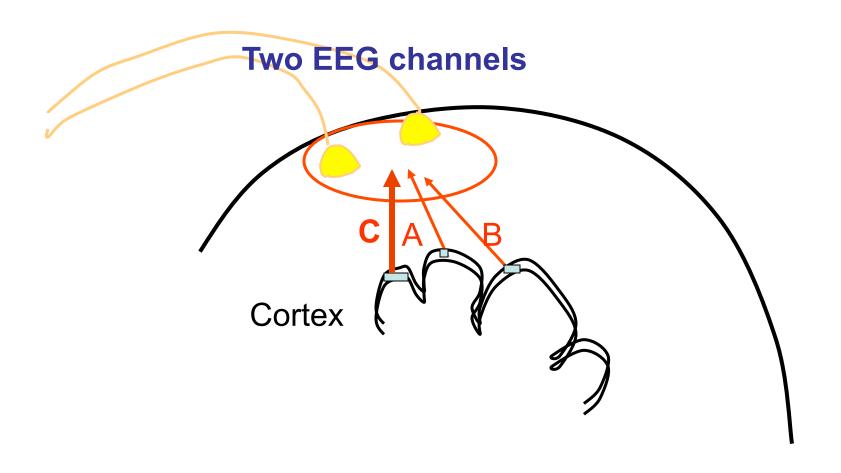
Only phase information component a

## Cross-coherence amplitude and phase

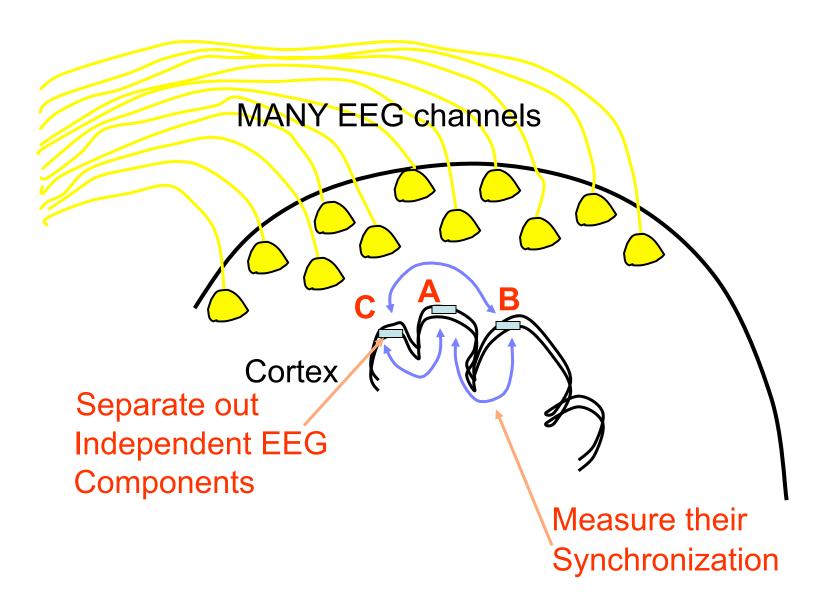






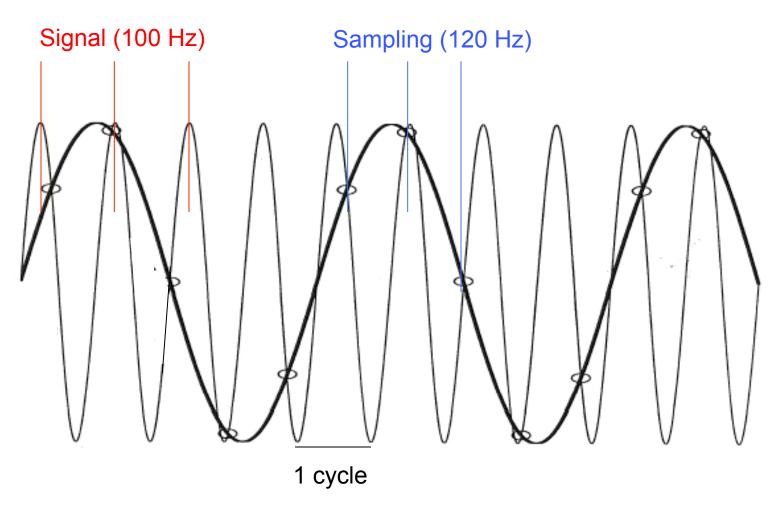


Scalp channel coherence → source confounds!



source dynamics!

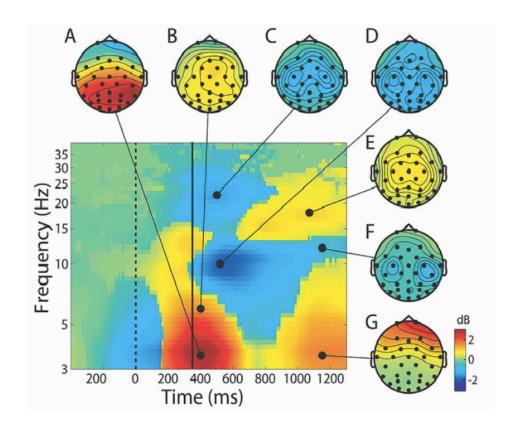
## Niquist frequency: Aliasing



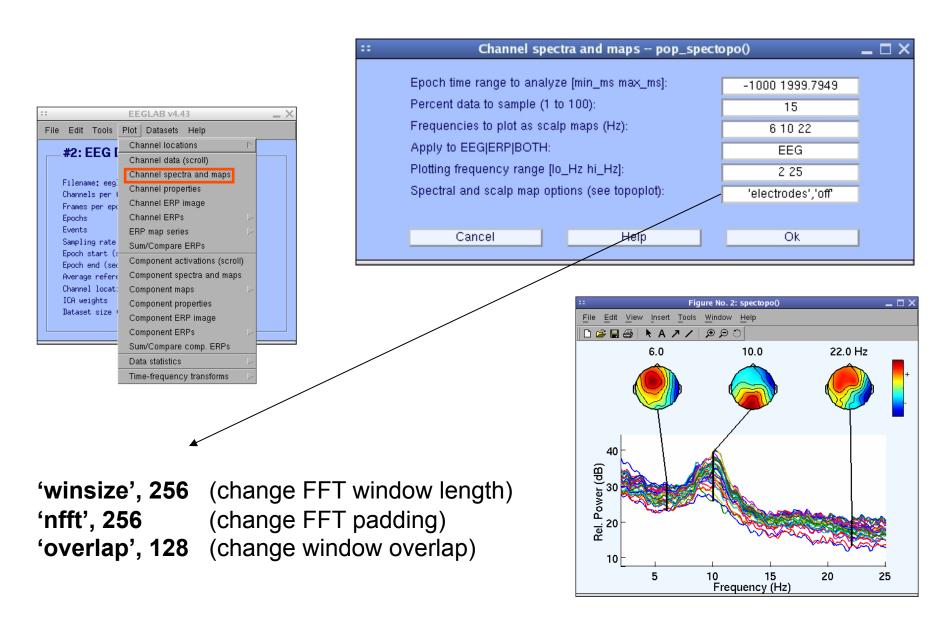
e.g. 100 Hz sampled at 120 Hz

# Advanced time-frequency functions

 Tftopo(): allow visualizing time-frequency power distribution over the scalp



## Plot data spectrum using EEGLAB



#### ALL

Start EEGLAB, from the menu load sample\_data/eeglab\_data\_epochs\_ica.set or your own data (epoch, reject noise if not done already)

#### Novice

From the GUI, Plot spectral decomposition with 100% data and 50% overlap ('overlap'). Try reducing window length ('winsize') and FFT length ('nfft')

#### Intermediate

Same as novice but using a command line call to the *pop\_spectopo()* function. Use GUI then history to see a standard call ("eegh").

#### Advanced

Same as novice but using a command line call to the *spectopo()* function.

#### **Exercise**

